# ME2 Computing- Coursework summary

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A) What physics are you trying to model and analyse? (Describe clearly, in words, what physical phenomenon you wish to analyse)

The physics of different types of insects hitting a spider’s web will be analysed with the use of the 1D wave equation. The initial conditions will be defined as the displacement of the web when the insect hits it and how the wave propagates from this point be evaluated. The 1D wave equation is being used as only a single piece of spider’s web is being investigated.

B) What PDE are you trying to solve, associated with the Physics described in A? (write the PDE)

This is the 1D wave equation and is a hyperbolic PDE. is the displacement of the web, is the distance along the web, is time and is the wave speed.

C) Boundary value and/or initial values for my specific problem: (be CONSISTENT with what you wrote in A)

The initial displacement will be based on a Gaussian pulse , where maximum displacement is derived from the speed of the insect at impact. Dirichlet boundary conditions are used where Initial velocity of the web is 0. is , (Justus, et al., 2022). Different insects have varying width, speed and weight.

D) What numerical method are you going to deploy and why? (Describe, in words, which method you intend to apply and why you have chosen it as opposed to other alternatives)

2 numerical methods will be used, 1 to solve the problem explicitly and the other implicitly. The explicit equation used was the central difference method. This method is good because it is simple to implement for the chosen equation and computationally efficient. However, CDM requires the CFL condition to be satisfied for the solution to be stable. This is to make sure that numerical information does not propagate faster than the physical wave speed. The implicit method used was the Crank-Nicolson method. Thus, benefitting from not needing the CFL condition to be met to ensure stability (this will be assessed later). Downsides, however, of implicit methods are the computational costs and the Crank-Nicolson method can introduce oscillations without damping and phase errors in wave propagation.

E) I am going to discretise my PDE as the following (show the steps from continuous to discrete equation and boundary/initial conditions:

Wave Equation (1D):

|  |  |  |
| --- | --- | --- |
|  |  | (1) |

Discretise:

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  |  | (2) |  | (3) |

Combining (2) and (3):

|  |  |  |
| --- | --- | --- |
|  |  | (4) |

Implementing Crank-Nicolson method and averaging to the ahead time step for :

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
|  | |  | | | (5) | | |
|  |  | | (6) | Substituting (6) into (5): | | (7) |

Rearranging (7) to form equation (8) for the matrix:

|  |  |  |
| --- | --- | --- |
|  |  | (8) |

G) Other remarks (limits of the model, convergence problems, possible alternative approaches, anything you find relevant and important to mention):

F) Plot the numerical results comprehensively and discuss them (discuss how the results describe the physics and comment on any discrepancies or unexpected behaviours). Use multiple types of visual graphs.